

数学与系统科学研究院

计算数学所学术报告

报告人: **Dr. Yong Zhang**

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报告题目:

**Analysis-based fast algorithms for  
convolution-type nonlocal potential  
in Nonlinear Schrödinger equation**

邀请人: 刘歆 副研究员

报告时间: 2017 年 5 月 18 日 (周四)

上午 10:00-11:00

报告地点: 科技综合楼三层

311 报告厅

## **Abstract:**

Convolution-type potentials are common and important in many science and engineering fields. Efficient and accurate evaluation of such nonlocal potentials are essential in practical simulations. In this talk, I will focus on those arising from quantum physics/chemistry and lightning-shield protection, including Coulomb, dipolar and Yukawa potentials that are generated by isotropic and anisotropic smooth and fast-decaying density. The convolution kernel is usually singular or discontinuous at the origin and/or at the far field, and density might be anisotropic, which together present great challenges for numerics in both accuracy and efficiency. The state-of-art fast algorithms include Wavelet based Method (WavM), kernel truncation method (KTM), NonUniform-FFT based method (NUFFT) and Gaussian-Sum based method (GSM). Gaussian-sum/exponential-sum approximation and kernel truncation technique, combined with finite Fourier series and Taylor expansion, finally lead to a  $O(N \log N)$  fast algorithm achieving spectral accuracy. Applications to NLSE are reviewed.

**欢迎大家参加！**