

Math 231. Quiz 5 (24 minutes)
Brief Table of Laplace Transforms

Name: _____

Function	Example
$\mathcal{L}[0] = 0$	N/A
$\mathcal{L}[c] = \frac{c}{s}$	$\mathcal{L}[231] = \frac{231}{s}$
$\mathcal{L}[t^n] = \frac{n!}{s^{n+1}}$	$\mathcal{L}[t^3] = \frac{3!}{s^4}$
$\mathcal{L}[e^{at}] = \frac{1}{s-a}$	$\mathcal{L}[e^{5t}] = \frac{1}{s-5}$
$\mathcal{L}[e^{at}t^n] = \frac{n!}{(s-a)^{n+1}}$	$\mathcal{L}[e^{2t}t^4] = \frac{4!}{(s-2)^5}$
$\mathcal{L}[\cos(bt)] = \frac{s}{s^2+b^2}$	$\mathcal{L}[\cos(7t)] = \frac{s}{s^2+49}$
$\mathcal{L}[\sin(bt)] = \frac{b}{s^2+b^2}$	$\mathcal{L}[\sin(7t)] = \frac{7}{s^2+49}$
$\mathcal{L}[e^{at} \cos(bt)] = \frac{s-a}{(s-a)^2+b^2}$	$\mathcal{L}[e^{5t} \cos(3t)] = \frac{s-5}{(s-5)^2+9}$
$\mathcal{L}[e^{at} \sin(bt)] = \frac{b}{(s-a)^2+b^2}$	$\mathcal{L}[e^{5t} \sin(3t)] = \frac{3}{(s-5)^2+9}$
$\mathcal{L}[af(t) + bg(t)] = a\mathcal{L}[f(t)] + b\mathcal{L}[g(t)]$	$\mathcal{L}[2 + 5t] = \mathcal{L}[2] + 5\mathcal{L}[t] = \frac{2}{s} + 5\left(\frac{1}{s^2}\right)$

1. (6 points) Compute $\mathcal{L}[2e^{-t} - 3e^{2t} \cos(t)]$.

2. Compute the inverse Laplace transforms.

(a) (7 points) $\mathcal{L}^{-1} \left[\frac{3}{s^3} + \frac{2s+1}{s^2+4} \right]$

(b) (7 points) $\mathcal{L}^{-1} \left[\frac{3s+1}{s^2-1} \right]$